Objective 10. Apply equilibrium principles to insoluble solids.

Key ideas:

Chem 1A: ionic solids are either soluble or insoluble. See solubility rules table.

Chem 1B: insoluble solids are slightly soluble.

AB (s) $\leq = A^+$ (aq) + B^- (aq). K_{sp} is K_{eq} for this reaction. $K_{sp} = [A^+][B^-]$

- 1. A high concentration of Ca²⁺ and Mg²⁺ ions makes water hard. Hard water causes unsightly spots on cups and glasses and stains on bathroom surfaces. These hard water stains are Ca(OH)₂ and Mg(OH)₂.
- a. What chemical force is involved in making these two compounds insoluble in water?
- b. When Ca(OH)₂ is in water, this solid is in equilibrium with its ions:

$$Ca(OH)_2$$
 (s) <==> Ca^{2+} (aq) + 2 OH^- (aq)

The equilibrium constant for this reaction is called the solubility product equilibrium constant, K_{so}. For Ca(OH)₂, $K_{sp} = [Ca^{2+}(aq)][OH^{-}(aq)]^{2}$. Note: Ca(OH)₂ (s) is a pure substance so $[Ca(OH)_{2}(s)] = 1$. The K_{sp} of Ca(OH)₂ is 4.7x10⁻⁶. The K_{sp} of Mg(OH)₂ is 5.6x10⁻¹². (Note: A Table of K_{sp} values of ionic solids is in the textbook.)

Which compound is more soluble in water? Give reasons.

- c. Under what conditions will a precipitate form?
 - i.

 - $[Ca^{2+} (aq)] [OH (aq)]^2 < 4.7x10^6$. $[Ca^{2+} (aq)] [OH (aq)]^2 = 4.7x10^6$. $[Ca^{2+} (aq)] [OH (aq)]^2 > 4.7x10^6$.

Under what conditions is the solution saturated?

- d. See Question 5d for how to get rid of hard water stains.
- 2. BaSO₄ is used in medicine to diagnose digestive tract disorders. A patient ingests a mixture of BaSO₄ in water. The insoluble BaSO₄ helps image the patient's intestines when x-rayed. However, the presence of sulfate in water could lead to laxative effects if the concentration of sulfate exceeds 250 mg/l. You add 1 mole of BaSO₄ to 1 liter of water.
- a. Write a chemical equation that represents the equilibrium of BaSO₄ solid with its ions.

$$BaSO_4$$
 (s) <===> Ba^{2+} (aq) + ??

- b. Write an equilibrium constant expression for this reaction. Note: BaSO₄ (s) is a pure substance so $[BaSO_4 (s)] = 1.$
- c. Under what conditions will a precipitate form?
 - $[Ba^{2^{+}}(aq)][SO_{4}^{2^{-}}(aq)] < K_{sp}$ $[Ba^{2^{+}}(aq)][SO_{4}^{2^{-}}(aq)] = K_{sp}$ $[Ba^{2^{+}}(aq)][SO_{4}^{2^{-}}(aq)] > K_{sp}$
 - ii.

Under what conditions is the solution saturated?

- d. Look up K_{sp} (solubility product equilibrium constant) for BaSO₄.
- e. Set up an equilibrium calculation.
- f. What is the mass of 1 mole of BaSO₄?
- g. Calculate the molar concentration of sulfate when 1 mole of BaSO₄ is added to 1 liter of water.
- h. Calculate the sulfate concentration in mg/liter. (Answer: between 0.5 and 1.5 mg SO₄²⁻/l)
- i. Will a BaSO₄ shake cause diarrhea? Give reasons.
- 3. You know that calcium carbonate is insoluble in water from Chem 1A. However, according to solubility equilibria, calcium carbonate solid is in equilibrium with its ions. In other words, a small amount of calcium carbonate does dissolve in water.
- 1 mole of calcium carbonate is dumped in 1 liter of water.
- a. Write a chemical equation that represents the equilibrium of calcium carbonate solid with its ions.

$$CaCO_3$$
 (s) <===> Ca^{2+} (aq) + ??

- b. Look up K_{sp} (solubility product equilibrium constant) for calcium carbonate.
- c. Set up an equilibrium calculation.
- d. What is the mass of 1 mole of CaCO₃?
- e. Calculate the concentration of Ca²⁺ ion in this solution. (Answer: between 1 and 3 mg Ca²⁺/l)
- f. Our drinking water flows over limestone (CaCO₃) rocks before it is treated to make drinkable. Hard water contains Ca²⁺ and Mg²⁺. How does water get hard?
- 4. Calcium carbonate is insoluble in water. But you can make CaCO₃ soluble by adding acid.
- a. When HCl is added to CaCO₃, which direction does the reaction shift? Use LeChatelier's principle to support your answer. Is a reactant or product being added or removed?

$$CaCO_3$$
 (s) <===> Ca^{2+} (aq) + CO_3^{2-} (aq)

- b. You know that calcium carbonate dissolves in HCl. Write a balanced chemical equation and net ionic equation that represents this reaction.
- c. The equilibrium constant for the reaction in (b) is greater than 1. Explain why.
- d. When vinegar (acetic acid) is added to $CaCO_3$, which direction does the reaction shift? Use LeChatelier's principle to support your answer. Is a reactant or product being added or removed? $CaCO_3$ (s) <===> Ca^{2^+} (aq) + $CO_3^{2^-}$ (aq)
- e. You know that calcium carbonate dissolves in acetic acid. Write a balanced chemical equation and net ionic equation that represents this reaction.
- f. The equilibrium constant for the reaction in (e) is greater than 1. Explain why.
- g. Most carbonate salts are insoluble in water. What substance can you use to dissolve an insoluble carbonate solid?
- 5. Magnesium hydroxide is used in Milk of Magnesia as an antacid. The hard water stains on your kitchen glasses and cups are calcium hydroxide. Most hydroxide salts are insoluble in water (see Solubility Table from Chem 1A).
- a. Write a chemical equation that represents the equilibrium between a hydroxide salt, MOH (s), and its aqueous ions.
- b. K_{eq} for your reaction in (a) is less than 1. Explain why.
- c. What substance could you add to dissolve a hydroxide salt? Use LeChatelier's principle to support your answer. Is a reactant or product being added or removed?
- d. A hard water stain is Ca(OH)₂. What common household substance would you use to get rid of hard water stains? Apply LeChatelier's principle to support your answer. Is a reactant or product being added or removed?
- 6. If the pH of a swimming pool is too acidic, it corrodes the pool surfaces, such as marble.
- a. Marble is calcium carbonate. Is $CaCO_3$ soluble in water? What numerical quantity tells you this information? Give the numerical value of this quantity to support your answer.
- b. What observation tells you acid reacts with marble? Write a chemical equation that represents the reaction between marble and acid. Use HCl for the acid.
- 7. The active ingredient in Milk of Magnesia antacid is Mg(OH)₂. This compound is not soluble in water.
- a. Write a chemical equation that represents the equilibrium between Mg(OH)₂ (s) and its aqueous ions.
- b. What numerical quantity tells you Mg(OH)₂ is not soluble in water? Give the numerical value of this quantity to support your answer.
- c. You have an upset stomach and take a dose of Milk of Magnesia. Will the $Mg(OH)_2$ dissolve when it gets in your stomach?
- (i) Use LeChatelier's principle on your chemical equation from (a) to determine the direction the reaction shifts when Mg(OH)₂ gets in your stomach.
- (ii) Write a chemical equation between the chemical in your stomach and Mg(OH)₂ to support your answer.